











	Boolean Algebra		
1b. $1+1=1$ 10a. $x \cdot y = y \cdot x$ (Lommutative)2a. $1 \cdot 1 = 1$ 10b. $x + y = y + x$ 2a. $1 \cdot 1 = 1$ 10b. $x + y = y + x$ 2b. $0 + 0 = 0$ 11b. $x + (y + z) = (x + y) + z$ 3a. $0 \cdot 1 = 1 \cdot 0 = 0$ 12b. $x + (y + z) = (x + y) + z$ 3b. $0 + 1 = 1 + 0 = 1$ 12b. $x + (y - z) = (x + y) \cdot (x + z)$ 4a. If $x = 0$ , then $x' = 1$ 13b. $x \cdot (y + z) = (x + y) \cdot (x + z)$ 4b. If $x = 1$ , then $x' = 0$ 13b. $x \cdot (x + y) = x$ 5b. $x + 1 = 1$ 14b. $(x + y) \cdot (x + y') = x$ 6a. $x \cdot 1 = x$ 15b. $(x + y)' = x' + y'$ 7b. $x + x = x$ 16a. $x + x' \cdot y = x + y$ 7b. $x + x = x$ 16b. $x \cdot (x' + y) = x \cdot y'$ 8a. $x \cdot x' = 0$ 16b. $x \cdot (x' + y) = x \cdot y$	<ul> <li>How do we use Boolean algebr</li> <li>1a. 0 · 0 = 0</li> </ul>	a to obtain fewest literals and ter	ms?
$6b. x + 0 = x$ $15a. (x \cdot y)' = x' + y'$ (DeMorgan's Theorem) $6b. x + 0 = x$ $15b. (x + y)' = x' + y'$ (DeMorgan's Theorem) $7a. x \cdot x = x$ $15b. (x + y)' = x' + y'$ (DeMorgan's Theorem) $7b. x + x = x$ $16a. x + x' \cdot y = x + y$ (DeMorgan's Theorem) $8a. x \cdot x' = 0$ $16b. x \cdot (x' + y) = x \cdot y$ $16b. x \cdot (x' + y) = x \cdot y$	1b. $1 + 1 = 1$ 2a. $1 \cdot 1 = 1$ 2b. $0 + 0 = 0$ 3a. $0 \cdot 1 = 1 \cdot 0 = 0$ 3b. $0 + 1 = 1 + 0 = 1$ 4a. If $x = 0$ , then $x' = 1$ 4b. If $x = 1$ , then $x' = 0$ 5a. $x \cdot 0 = 0$ 5b. $x + 1 = 1$ 6a. $y \cdot 1 = y$	10a. $x \cdot y = y \cdot x$ 10b. $x + y = y + x$ 11a. $x \cdot (y \cdot z) = (x \cdot y) \cdot z$ 11b. $x + (y + z) = (x + y) + z$ 12a. $x \cdot (y + z) = x + y + x \cdot z$ 12b. $x + (y \cdot z) = (x + y) \cdot (x + y)$ 13a. $x + x \cdot y = x$ 13b. $x \cdot (x + y) = x$ 14a. $x \cdot y + x \cdot y' = x$ 14b. $(x + y) \cdot (x + y') = x$	(Commutative) (Associative) (Distributive) + 2) (Absorption) (Combining)
8b. x + x' = 1 9. x'' = x	6a. $x \cdot 1 = x$ 6b. $x + 0 = x$ 7a. $x \cdot x = x$ 7b. $x + x = x$ 8a. $x \cdot x' = 0$ 8b. $x + x' = 1$ 9. $x'' = x$	15a. $(x \cdot y)' = x' + y'$ 15b. $(x + y)' = x' \cdot y'$ 16a. $x + x' \cdot y = x + y$ 16b. $x \cdot (x' + y) = x \cdot y$	(DeMorgan's Theorem)

























## 



































are each er f they differ l dd check to	try in Gi to each e y 1 bit, we can apply ninterm/implicant to	ntry in Gi- the uniting remind us t	+1 +1	πτ )				
f they differ l dd check to	y 1 bit, we can apply ninterm/implicant to	the uniting remind us t	, the					
dd check to	ninterm/implicant to	remind us t		eorem an	d eliminate	a literal		
			that	it is not	a prime imp	licant		
/ (0) 000	(0,2) ?	G0	1	(0,2)	00-0	-	G0	(0,2,4,6) 0-
(2) 001	(2,3) ?		1	(0,4)	0-00	-		(2 2 ( 7) 0
(2) 0010	(2,6) ?	G1	7	(2,3)	001-		GI	(2,3,6,7) 0-
(4) 010	(2,9) ? N		5	(2,6)	0-10	-	G2	(3,7,11,15)
/ (3) 001	(4,5)? N (4,6)?		Ŷ	(4,6)	01-0			(9,11,13,15) 1-
(6) 011	(4,9) ? N			(2.3)				
(9) 100	(3,7) ?	GZ	1	(3,7)	0-11			anto oro
(3,11) ?		1	(3,11)	-011	dener	enerated – end of step 1		
(7) 011	(6,7)?		1	(6,7)	011-	gonor		and of otop 1
(11) 101:	(6,11) ? N		1	(9,11)	10-1			
(13) 110	(6,13) ? N (9,7) ? N		1	(9,13)	1-01			
. (45) 4	(9,11) ?	G3	1	(7,15)	-111			
(15) 111	(9,13) ?		1	(11,15)	1-11			
	(0) 00000 (2) 0010 (4) 0100 (3) 0011 (6) 0110 (9) 1001 (7) 0111 (11) 1011 (13) 1101 (15) 1111	(0)         0000         (0,4) ?           (2)         0010         (2,3) ?           (2)         0010         (2,9) ? N           (4)         0100         (2,9) ? N           (3)         0011         (4,6) ?           (4)         0100         (3,7) ?           (4)         (3)         011           (4,6) ?         (4,6) ?           (9)         1001         (3,1) ?           (7)         0111         (5,1) ? N           (6,7) ? N         (13)         1101           (5,7) ? N         (9,1) ?           (15)         1111         (9,1) ?	(0) 0000         (0, 1)?         G0           (2) 0010         (2,3)?         (2,0)?           (4) 0100         (2,9)? N         G1           (3) 0011         (4,3)? N         (4,3)? N           (6) 0110         (4,9)? N         G2           (9) 1001         (3,1)?         G2           (7) 0111         (3,1)? N         G2           (11) 1011         (6,1)? N         G3           (13) 1101         (9,1)? N         G3           (15) 1111         (9,1)?         G3	(0)         0000         (0,4)?         G0           (2)         0010         (2,3)?         (2,6)?         G1           (4)         0100         (2,9)?N         G1         (4,3)?N           (3)         0011         (4,6)?         G1           (6)         0110         (4,9)?N         G2           (9)         1001         (3,7)?         G2           (7)         0111         (3,13)?N         (6,7)?           (11)         1011         (6,11)?N         (4,1)?N           (13)         1101         (6,13)?N         (6,7)?N           (13)         1101         (9,11)?         G3           (15)         1111         (9,13)?         G3	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$









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Petr	ick's Method – used to determine minimun	n cover			26/8	9 13 15
1.	Reduce prime implicant chart by		(2,6) (8,9)	-001		
	eliminating prime implicant rows and	P1	(6,7)	011-	T	1
	corresponding columns	P2	(9, 13)	10-1		<b>* *</b>
2.	Label rows of reduced prime implicant	P3	(7, 15)	-111	*	Τ΄ 😦
2	Chart P1, P2	P4	(13, 15)	1-11		* *
5.	all columns are covered			1		1
4.	Reduce to minimum sum of products by	P = (P1 +	P3)(P2 + I	P4)(P3 +	P4)	
	multiplying out and applying $X + XY = X$	P = (P1 +	P3)(P2P3			
5.	Each term in solution represents a		P4P4 = P4			
	covering solution	P = (P1 +	P4P3 + P4)	P4 + P4P3 = P4		
<ul> <li>Count number of terms in each, cho one corresponding to the minimum</li> </ul>	<ul> <li>Count number of terms in each, choose one corresponding to the minimum</li> </ul>	P = (P1 +	P4)			
	number	P = (P1 +		P4 + P2P4 = P4		
		, D - D400				
		F - F 1F2	P = P1P2P3 + P1P4 + P3P2P3 + P3P4			
		P = P1P2	P = P1P2P3 + P1P4 + P2P3 + P3P4			



