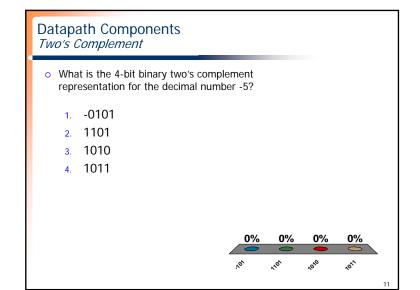
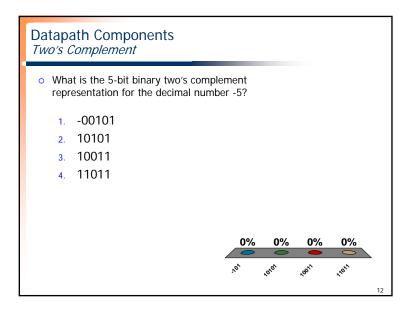


Two's Complement is Easy to Compute: Just Invert Bits and Add 1

• Hold on!

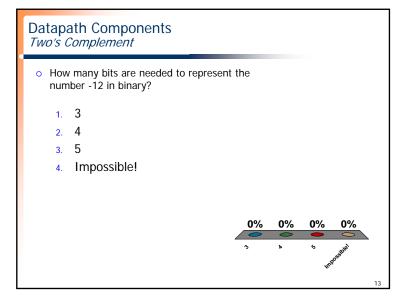
- □ Sure, adding the ten's complement achieves subtraction using addition only
- But don't we have to perform *subtraction* to determine the complement in the first place?
- True but in binary, two's complement can be computed easily
- □ Two's complement of 011 is 101, because 011 + 101 is 1000
- Could compute complement of 011 as 1000 011 = 101
- Easier method: Just invert all the bits, and add 1
- The complement of 011 is 100+1 = 101 it works!

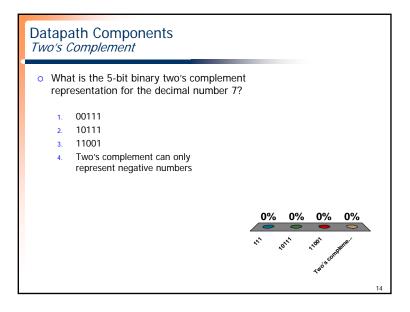


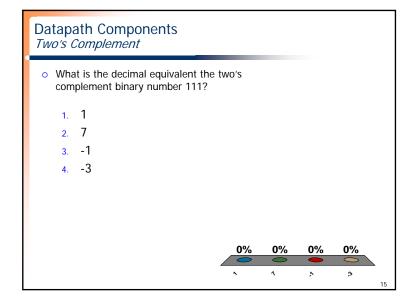


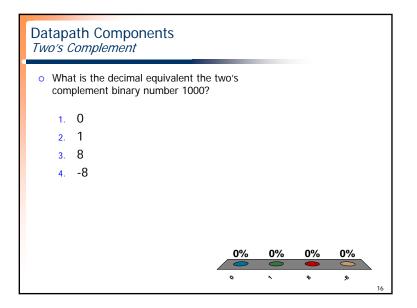
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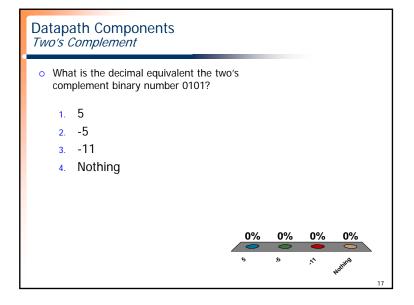
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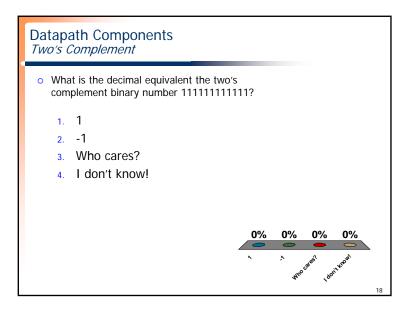


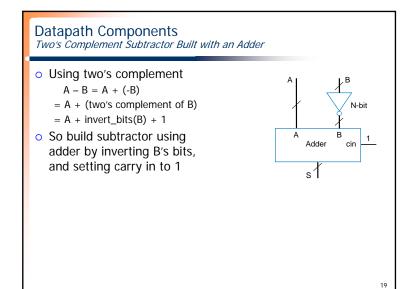


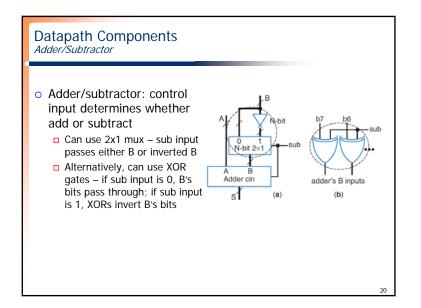










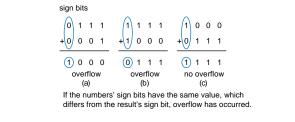


Datapath Components Overflow

- Sometimes result can't be represented with given number of bits
 - Either too large magnitude of positive or negative
 - □ e.g., 4-bit two's complement addition of 0111+0001 (7+1=8). But 4bit two's complement can't represent number >7
 - 0 0111+0001 = 1000 WRONG answer, 1000 in two's complement is -8, not +8
 - Adder/subtractor should indicate when overflow has occurred, so result can be discarded

Datapath Components Overflow: Detecting Overflow: Method 1

- Assuming 4-bit two's complement numbers, can detect overflow by detecting when the two numbers' sign bits are the same but are different from the result's sign bit
 - □ If the two numbers' sign bits are different, overflow is impossible
 - Adding a positive and negative can't exceed largest magnitude positive or negative
- Simple circuit
 - \square overflow = a3'b3's3 + a3b3s3'
 - Include "overflow" output bit on adder/subtractor



Datapath Components Overflow: Detecting Overflow: Method 2 • Even simpler method: Detect difference between carry-in to sign bit and carry-out from sign bit • Yields simpler circuit: overflow = c3 xor c4 0 0 0 0 0 0 1 1 1 0 1 1 1 1 1 1 1 1 0 0 0 +0 0 0 1 +1 0 0 0 +0 1 1 1 01000 10111 01111 no overflow overflow overflow (a) (b) (c) If the carry into the sign bit column differs from the carry out of that column, overflow has occurred.

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 ALU Component that can perform any of various arithmetic (add, subtract, increment, etc.) and logic (AND, OR, etc.) 	TABLE 4.2 Desired calculator operations				
	Inputs			Operation	Sample output if A=00001111,
operations, based on	х	У	Z		B=00000101
control inputs	0	0	0	S = A + B	S=00010100
	0	0	1	S = A - B	S=00001010
 Motivation: 	0	1	0	S = A + 1	S=00010000
Suppose want multi-	0	1	1	S = A	S=00001111
function calculator that	1	0	0	S = A AND B (bitwise AND)	S=00000101
not only adds and	1	0	1	S = A OR B (bitwise OR)	S=00001111
subtracts, but also	1	1	0	S = A XOR B (bitwise XOR)	S=00001010
increments, ANDs, ORs,	1	1	1	S = NOT A (bitwise complement)	S=11110000

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